

Parametric Analysis of the PGM Protocol

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1. Introduction

❖ Talk outline

1. Protocol PGM
2. Modeling PGM
3. Parametric Analysis
4. Verification
5. Conclusion



1. Protocol PGM

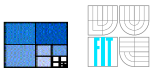
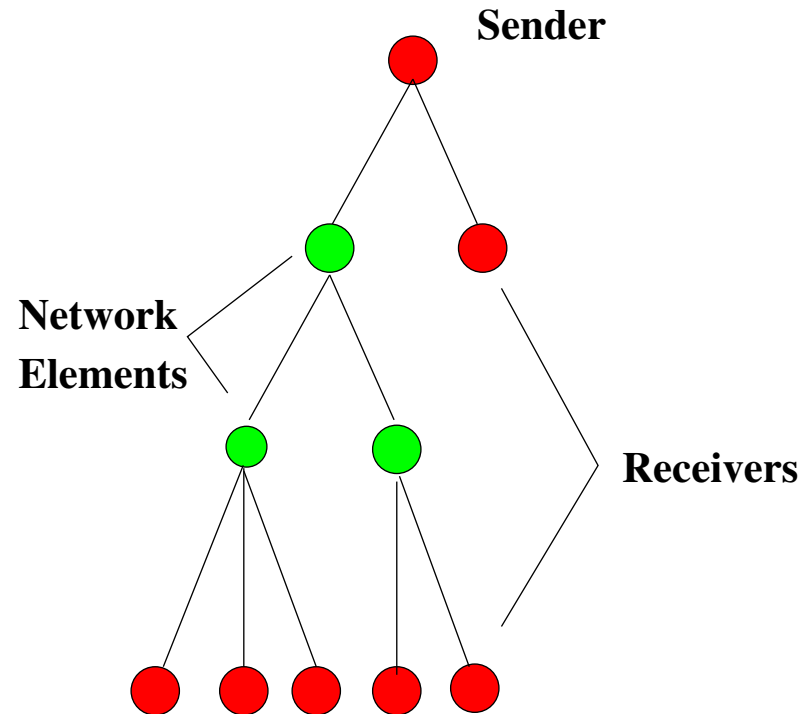
❖ General Overview

- **PGM (Pragmatic General Multicast) defined by RFC 3208.**
- **Reliable multicast transport protocol for application, that require ordered or unordered, duplicate-free, multicast data delivery from multiple sources to multiple receivers .**
- **Members may join and leave the group at any time.**
- **Many different types of data packets (ODATA, RDATA, SPMs, NAKs etc).**



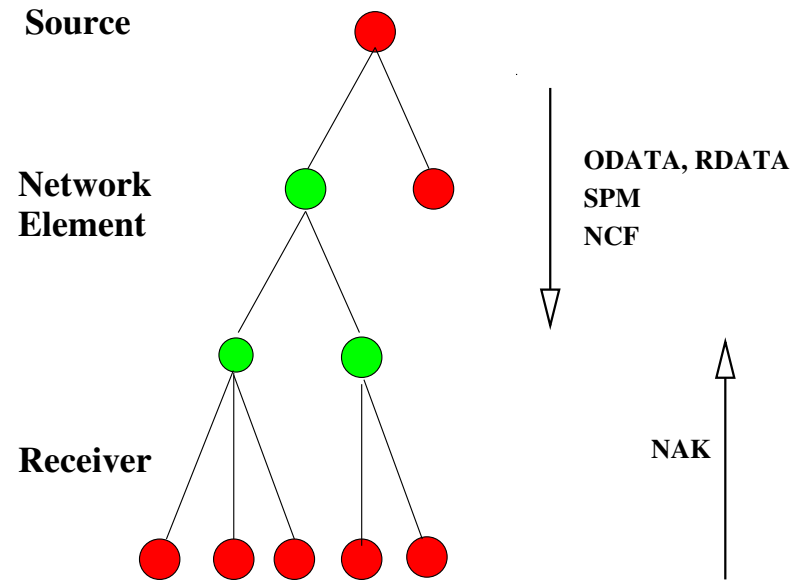
1. Protocol PGM - Introduction

❖ Protocol Architecture



1. Protocol PGM - Introduction

❖ Data Transmission



- **Data (ODATA, RDATA),**
- **SPM (Source Path Message),**
- **NAK (Repair request), NCF (NAK confirmation)**

2. Protocol PGM - Verification

- ❖ **PGM guarantees that "a receiver either receives all data packets from transmissions and repairs, or is able to detect unrecoverable data packet loss".**
- ❖ **Several verification studies on PGM has been done.**
- ❖ **B.Bérard, P.Bouyer, and A. Petit: Analysis the PGM protocol with UPPAAL. RT-TOOLS, August 2002.**
 - **Verification of a simplified timed version of PGM with linear topology and one-placed buffer.**
 - **The reliability property of the protocol is verified by instantiating the parameters and calling the UPPAAL tool.**
 - **Verification of two properties:**



2. Protocol PGM - Verification [BBP]

❖ **Lost info property** - “For each data, each receiver knows if it did receive the data or if it will never receive it”.

- **960 control states, 5 clocks, 25 bounded variables**
- **Property $E \langle \rangle (\text{obs}.\text{Error})$ is True means the receiver may make mistake to estimate restoration of a data.**

❖ **No-loss property** - “Each data which is detected as lost is eventually repaired”.

- **17280 control states, 5 clocks, 35 bounded variables**
- **Property $E \langle \rangle (\text{receiver1.test}==1 \text{ ro } \text{receiver2.test}==2)$ is True, that means it is not verified.**



1. Protocol PGM - Verification [BS]

❖ **M.Boyer, M.Sighireanu: Synthesis and verification of constraints in the PGM protocol. FME, September 2003. (ADVANCE, 2nd year)**

- **Verification of the PGM using classical tools (IF, CADP).**
- **Manual synthesis of the constraints between parameters.**
- **Verification of full reliability property using T_{REX} .**
- **Property verified by instantiation of parameters.**
- **Analysis of complexity - addressing of sources of complexity.**

❖ **Our goal: To obtain the constraint deduced in this work automatically.**



1. Protocol PGM - Verification [BS]

❖ **Losses-signaled property** - “a receiver either receives all data packets and repairs, or is able to detect unrecoverable data packet loss”.

- The property was verified for all messages, except for those of the last transmission window - a problem of closing window.
- The problem can be solved using “closing SPM ”.

❖ **Parametric analysis of full reliability property** - finding a relation between parameters of the system that satisfies the property.

- The relation (a constraint with parameters) was manually derived.
- The property was successfully verified using instantiation of the parameters - the result confirmed the property.



1. Protocol PGM - Verification [others]

❖ **P.Boigelot, L.Latour: Verifying PGM with infinitely many packets. LIAFA 2002.**

- **Validation using LASH of the sliding window mechanism of the protocol for any number of data packets sent.**
- **Different model based on finite state automata - no time model.**
- **Study the relation between the LEAD and TRAIL values of the Transmit Window and Receive Window.**

❖ **J.Esparza, M.Maidl: Simple representative instantiations for multicast protocols. TACAS, 2003.**

- **Mathematical framework for multicast protocol that allows to generalize the results obtained for linear topologies to tree topologies.**



2. Modeling PGM

❖ Analysing the full PGM protocol is **beyond limits of current verification tools** because of

- **dynamic topology - joining/leaving a node,**
- **multiple senders,**
- **a lot of different packet types (SPMs, NCF , NAKs),**
- **a lot of processes, counters and clocks.**

❖ **Sources of complexity:**

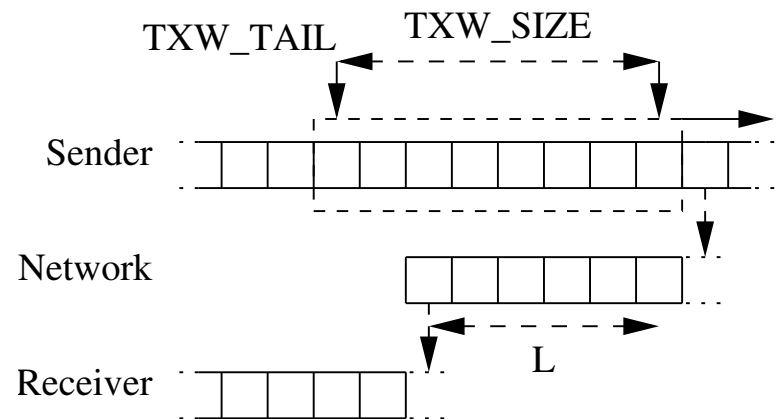
- **many variables,**
- **non-linear constraints.**

❖ **We need a new abstract model.**



2. Modeling PGM - An abstract model

❖ The abstract model is based on a global view of the protocol running between the sender and one of the receivers



- **Linear topology - a sender, network, a receiver.**
- **Network is abstracted into unreliable, unbounded FIFO queue implemented by a counter automaton.**
- **Only data packets (ODATA) are transmitted.**

2. Modeling PGM - The abstract model

❖ **Global view abstraction reduces number of counters and variables.**

❖ **Clocks, counters, variables:**

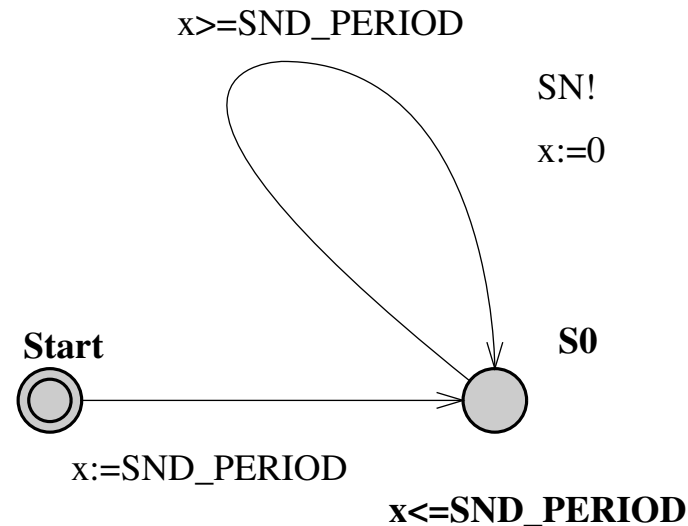
- **two clocks - x, y , two counters - L, def_lost ,**
- **one finite variables - lp ,**
- **six parameters - RATE, NLOSS, TXW_SIZE, BUFFER_LENGTH, SND_PERIOD, CH_PERIOD.**



2. Modeling PGM - The sender

❖ The sender

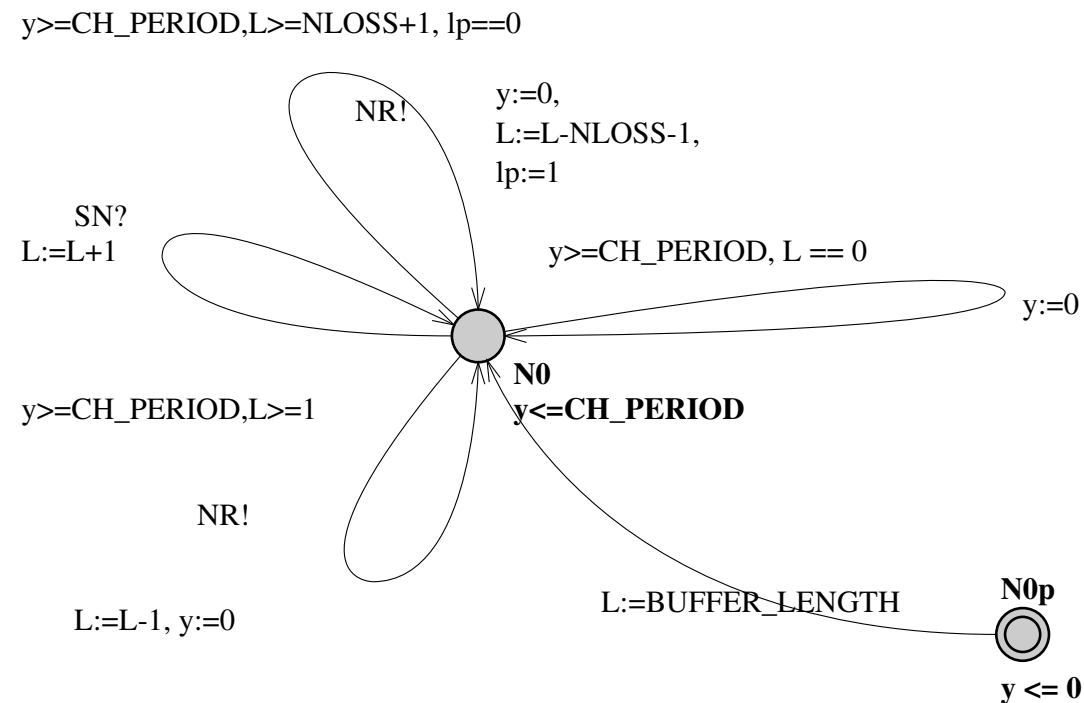
- generates ODATA packets each `SND_PERIOD`,
- advances transmitting window by one after each data packet is sent.
- The transmit window is fixed in order to save data as long as possible.



2. Modeling PGM - The network

❖ The network

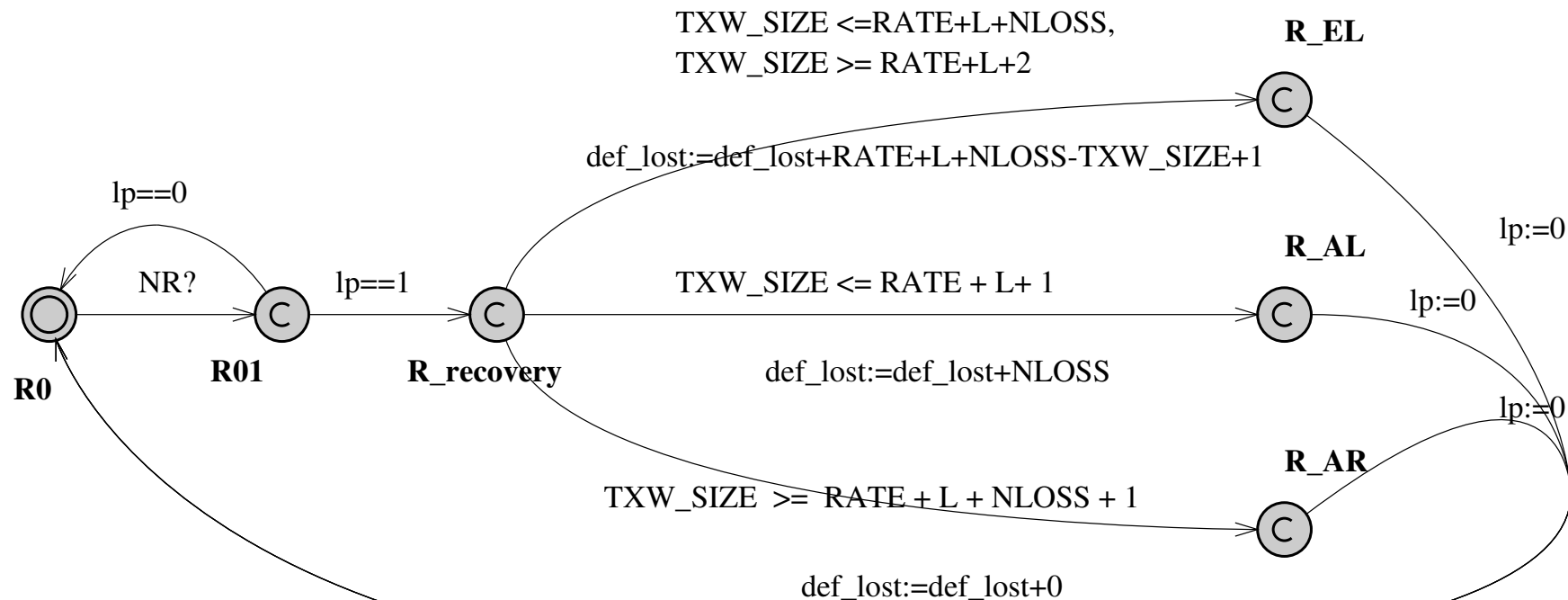
- receives data from the sender,
- delivers data to the receiver each `CH_PERIOD`,
- non-deterministically generates losses of `NLOSS` packets (variable `lp`)



2. Modeling PGM - The receiver

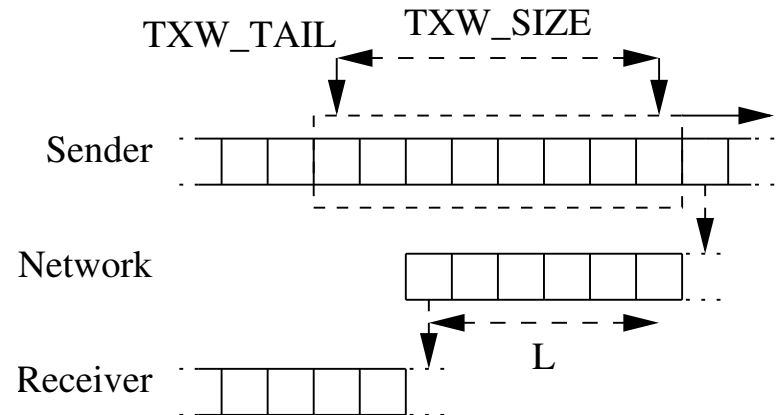
❖ The receiver

- accepts data from the network,
- detects losses - computes if lost packets can be recovered.
- **RATE** is ratio between the transmission speed and **SND_PERIOD**.



2. Modeling PGM - Detection of losses

❖ Global view abstraction



$\forall R$ All lost packets may be recovered if

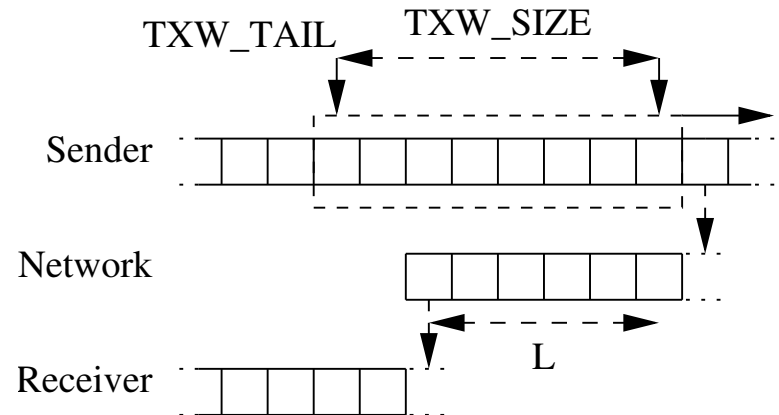
$$\text{TXW_SIZE} > \text{RATE} + L' + \text{NLOSS}$$

$\forall L$ None of the NLOSS lost packets may be recovered if

$$\text{TXW_SIZE} \leq \text{RATE} + L' + 1$$

2. Modeling PGM - Detection of losses

❖ Global view abstraction



$\exists R$ Some of the lost packets may be recovered if

$$\mathbf{TXW_SIZE} > \mathbf{RATE} + L' + 1$$

$$\mathbf{TXW_SIZE} \leq \mathbf{RATE} + L' + \mathbf{NLOSS}$$

❖ Only first relation satisfies the full reliability property.



3. Parametric Analysis

❖ All lost packet may be recovered if

$$\text{TXW_SIZE} > \text{RATE} + L' + \text{NLOSS}$$

where L' (the current value of L) is a variable, where $L' = L - \text{NLOSS} - 1$.

⇒ This constraint must be satisfied by the parameters in order to obtain full reliability.

❖ But L is a variable - we need a relation depending only on time and parameters.

❖ L can be computed as follows

$$L = f(t, \text{BUFFER_LENGTH}, \text{SND_PERIOD}, \text{CH_PERIOD}, \text{NLOSS})$$



3. Parametric Analysis

❖ To compute L , we distinguish four cases:

Case 1 $\text{SND_PERIOD} > \text{CH_PERIOD}$

- The rate of arrivals is less than departures.
- The size of the queue converges to zero by time.

$$0 \leq L \leq \text{BUFFER_LENGTH}$$

Case 2 $\text{SND_PERIOD} = \text{CH_PERIOD}$

- Arrivals are the same speed as departures.
- The size of the queue decreases to a value less than NLOSS because of losses.

$$0 \leq L \leq \text{BUFFER_LENGTH}$$



3. Parametric Analysis

Case 3 $\text{CH_PERIOD}/\text{SND_PERIOD} > \text{NLOSS}$

- Arrivals are faster than the sum of departures and losses.
- The queue grows beyond any limits by time.

$$\text{BUFFER_LENGTH} \leq L < \infty$$

Case 4 $\text{NLOSS} > \text{CH_PERIOD}/\text{SND_PERIOD} > 1$

- Arrivals are faster than departures, but not enough to fill the losses between two delivery.
- The queue is alternating depending on non-deterministic losses.

$$0 \leq L < \infty$$



3. Parametric Analysis - Constraints

❖ After substitution of L' and using limits on L we get following constraints:

❖ The constraint for full recovery is

$$\text{SND_PERIOD} \geq \text{CH_PERIOD} \wedge \text{TXW_SIZE} \geq \text{RATE} + \text{BUFFER_LENGTH}$$

❖ Partial recovery of losses is possible if

$$\text{TXW_SIZE} > \text{RATE} + \text{BUFFER_LENGTH} - \text{NLOSS}$$

❖ None of losses may be recovered if

$$\text{TXW_SIZE} \leq \text{RATE} + \text{BUFFER_LENGTH} - \text{NLOSS}$$



3. Parametric Analysis - Conclusion

❖ The constraints between parameters and the law of evolution of L are **non-linear relations on reals and integers.**

- For instance, exact value of L for case 3 is

$$L = \text{BUFFER_LENGTH} + \left\lceil \frac{t}{\text{CH_PERIOD}} \right\rceil \left\lceil \frac{\text{CH_PERIOD}}{\text{SND_PERIOD}} - 1 - \text{NLOSS} \right\rceil$$

❖ Verification can be done

- by instantiating some of parameters to avoid non-linear constraints,
- by applying acceleration,
- by applying approximation.



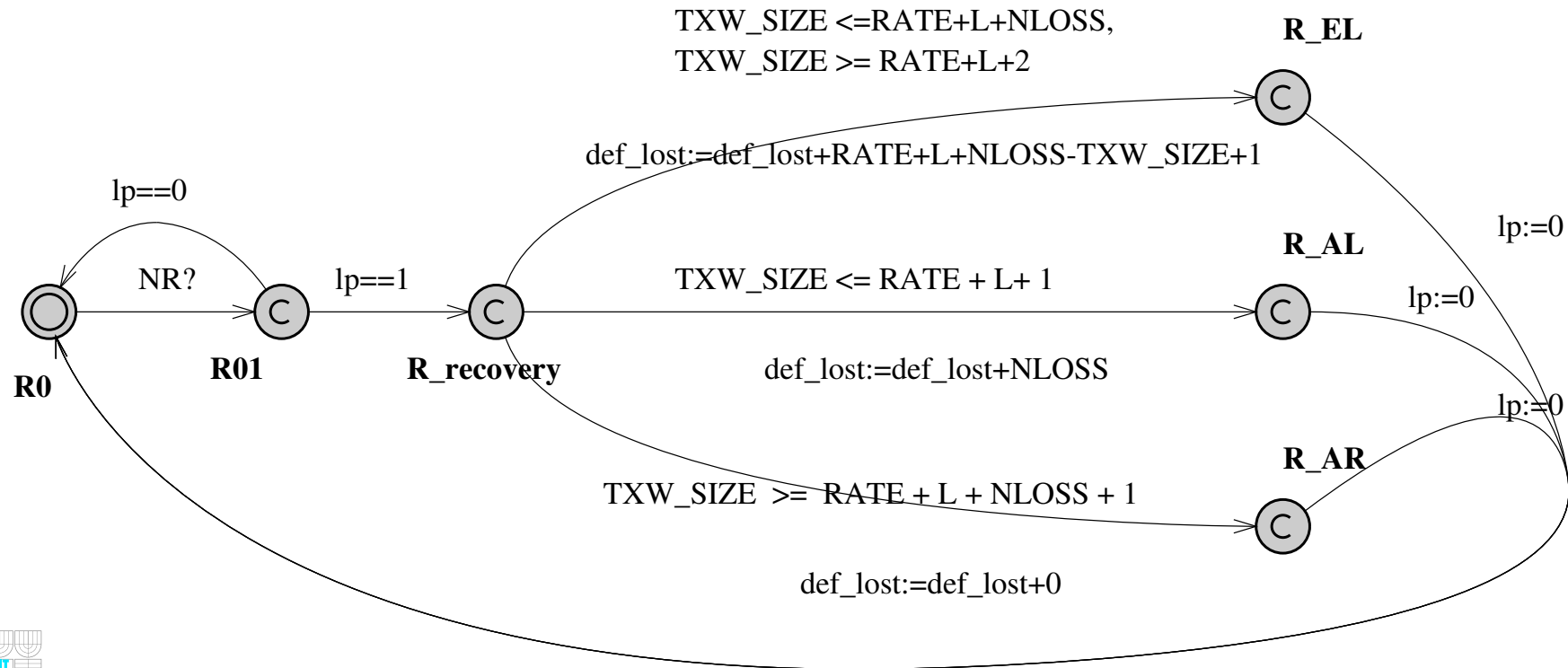
4. Verification - One Time Loss Model

- ❖ **Full reliability property** - “a receiver either receives all data packets or it is able to recover all lost data packets.”
- ❖ **“One Time Loss” Model**
 - Modified model where a loss appeared just once per session.
 - Non-linearities reduced using instantiation of some parameters.
 - To speed up analysis we carefully set initial conditions.
- ❖ **For parametric verification of the model we use HYTECH and TREN**



4. Verification - One Time Loss Model

- Three extended TA communicating via synchronization - the sender, the network, the modified receiver.
- One finite variable (lp), two clocks (x,y), two counters (def_lost, L).
- Six parameters.



4. Verification - using HYTECH

❖ Parametric verification using HYTECH

- HYTECH is a tool for parametric verification of hybrid systems.
- HYTECH does not support acceleration - generation of full reachability set does not terminate.
- To test our property we need to define a final region
`final_reg := def_lost > 0`
where the property is violated.
- We can get only results where the property is not satisfied.

❖ HYTECH output (for partial losses, $CH_PERIOD/SND_PERIOD \geq 2$)

RATE ≥ 1 & **SND_PERIOD** ≥ 1 & **BUFFER_LENGTH** ≥ 1 &
CH_PERIOD ≤ 2 **SND_PERIOD** &
TXW_SIZE + **NLOSS** \geq **RATE** + **BUFFER_LENGTH** + 3 &
SND_PERIOD < **CH_PERIOD** & **NLOSS** \leq **BUFFER_LENGTH** + 1
& **TXW_SIZE** \leq **RATE** + **BUFFER_LENGTH** + 2



4. Verification - using T_{REX}

- T_{REX} is a tool for parametric verification of timed systems.
- Model is based on extended timed automata.
- T_{REX} generates a set of reachable configuration for the input model and finite symbolic graph.
- It uses efficient extrapolation techniques to accelerate computation:

$$C = \{2 \leq x \leq 6, 1 \leq y \leq 4\}$$

$$post_{\theta}(C) = \{2 \leq x \leq 6, 1 \leq y \leq 6\}$$

$$post_{\theta}^2(C) = \{2 \leq x \leq 6, 1 \leq y \leq 8\}$$

$$post_{\theta}^*(C) = \{2 \leq x \leq 6, 1 \leq y \leq 4 + 2 * n\} \text{ using periodicity}$$

- Data structure in T_{REX} are represented using Parametric DBMs (PDBMs).



4. Verification - using TREX

❖ Case 1: $SND_PERIOD > CH_PERIOD$

- **R_AR**

$txw_size \geq rate + buffer_length$
and $buffer_length \geq nloss + 1$

- **R_EL**

$txw_size \geq rate + buffer_length - nloss - n3 - 1$ and
 $twx_size \leq rate + buffer_length - n3 - 3$ and
 $buffer_length \geq nloss + n3 - 3$ and
 $buffer_length \geq n3 - 2$ and
 $n3 \geq 0$

- **R_AL**

$txw_size \leq rate - nloss + buffer_length - n3 - 1$ and
 $buffer_length \geq nloss + n3 - 2$ and
 $buffer_length - n3 - 1 \leq 0$ and
 $n3 \geq 0$



4. Verification - using T_{REX}

❖ Case 2: $\text{SND_PERIOD} = \text{CH_PERIOD}$

- **R_{AR}**

$$\text{txw_size} \geq \text{rate} + \text{buffer_length}$$

- **R_{EL}**

$$\text{txw_size} \geq \text{rate} + \text{buffer_length} - \text{nloss} + 1 \text{ and}$$

$$\text{twx_size} \leq \text{rate} + \text{buffer_length} - 1$$

- **R_{AL}**

$$\text{txw_size} \leq \text{rate} - \text{nloss} + \text{buffer_length}$$

❖ No acceleration needed in this case.



4. Verification - using T_{REX}

❖ Case 3: $\text{CH_PERIOD}/\text{SND_PERIOD} > \text{NLOSS}$

- New parameter $q = \text{CH_PERIOD}/\text{SND_PERIOD}$, we consider $q \geq 2$
- Constraints similar like in the first case.

❖ Case 4: $\text{NLOSS} > \text{CH_PERIOD}/\text{SND_PERIOD} > 1$

- The experiments results are similar to the third case.



4. Verification - Conclusion

- ❖ **We successfully verified One Loss Time Model**
- ❖ **Analysis of the Full Abstract Model**
 - **There is no way to always recover losses in case 3 and case 4.**
 - **This can be done by searching a graph of symbolic configurations where $def_lost = 0$.**
 - **The problem is to generate this graph - L is complex, so the automatic computation fails.**
- ❖ **Another interesting point - the number of definitively lost packets**
 - **To compute that number we need a class of assignments for counters - not possible for DBMs.**
- ❖ **We need another data structure !**



5. Conclusion

❖ Future direction - parametrized intervals

- Based on Interval Diagrams extended with parameters.
- Domain is a vector (like PDBMs) with pair of bounds.
- New abstract data structure - p-hcubes
 - used for representation of configurations on counters (PDBMs for clocks)
 - space representation in $O(n)$ - better than PDBMs $O(n^2)$
 - canonical representation

❖ It will be a part of a new version of TReX.



5. Conclusion

❖ Parametric verification of PGM protocol

1. **New abstract model of PGM protocol based on global view of the system.**
2. **Parametric analysis of the system**
 - **Synthesis of constraints on parameters that satisfies the full reliability property.**
 - **Detection of non-linear relations between parameters \Rightarrow instantiation.**
 - **“One time loss” model.**
3. **Full automatic verification of the model with parameters using T_{REX} and H_YT_EC_H .**
4. **To verify Full Abstract Model we need a new data structure - we propose parametrized intervals.**

