

Contexts of parsing decisions

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Outline

- 1 Left context
- 2 DR-automata
- 3 Summary
- 4 Right Context
- 5 LR-regular

Left context

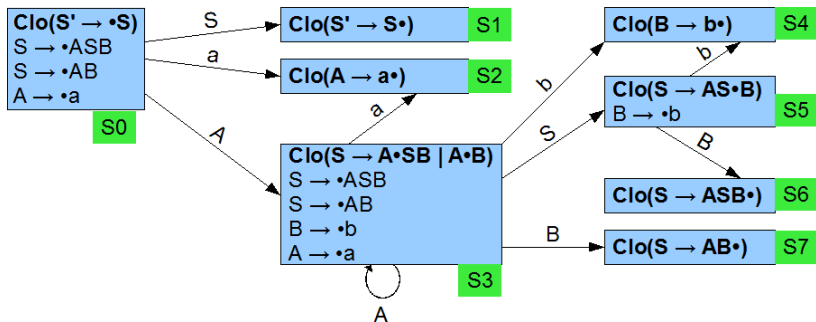
Definition, attributes

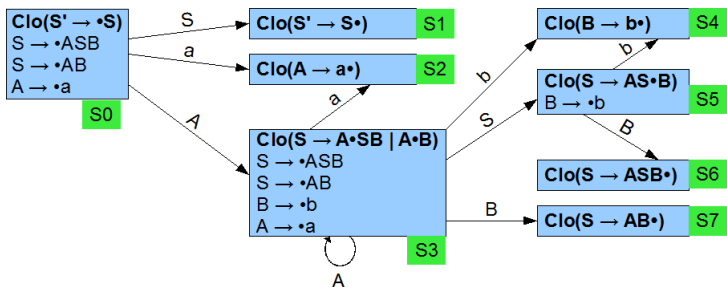
- Bound to a **state**
- Describes all possible stack configurations in that state
- Set of all strings of symbols ($N \cup T$) that lead to that state
- Usually infinite, but **regular**
- Contexts are **disjoint** across states
- We omit the state information

Left context - Example

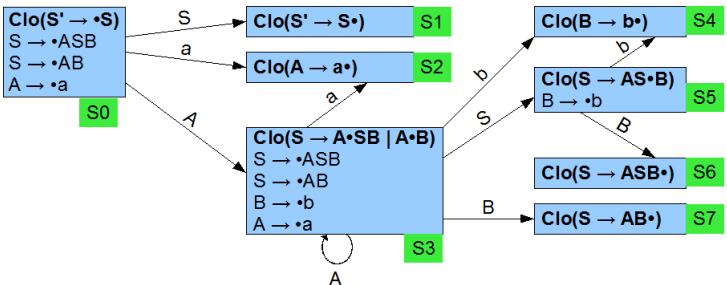
Example CFG $G = (N, T, P, S')$

- $N = \{S', S, A, B\}$
- $T = \{a, b\}$
- $P = \{S' \rightarrow S, S \rightarrow ASB \mid AB, A \rightarrow a, B \rightarrow b\}$
- $L(G) = a^n b^n$



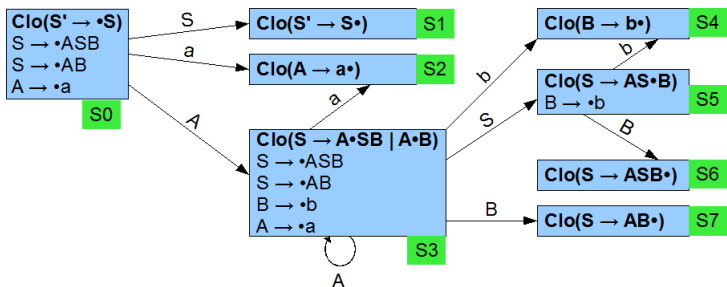


Grammar for left contexts



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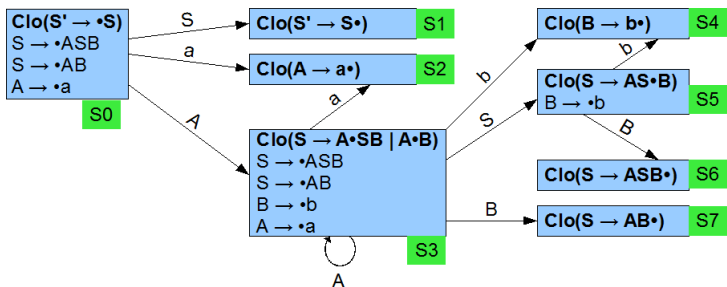
$$G = (N = \{P_{0..7}\}, T = \{S, A, B, a, b\}, P, S)$$



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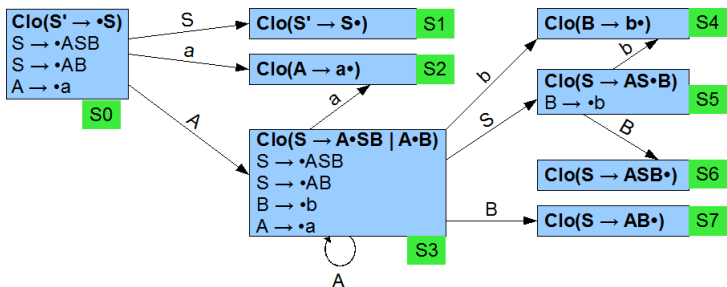
- $P_0 \rightarrow \epsilon$



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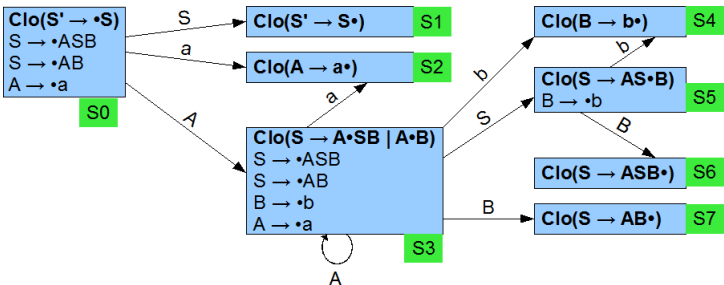
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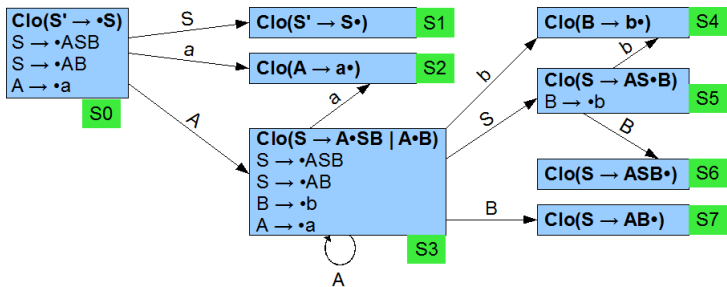
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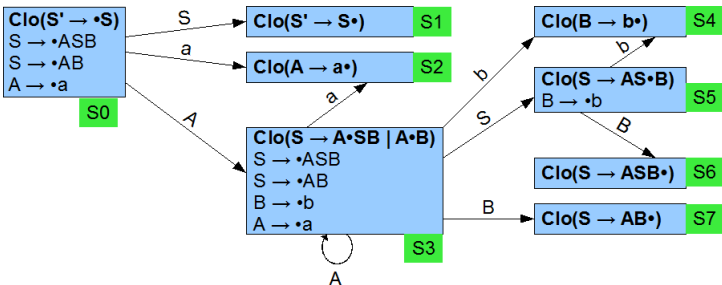
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- $P_3 \rightarrow P_0 A$
- $P_3 \rightarrow P_3 A$
- $P_4 \rightarrow P_3 b \mid P_5 b$
- $P_5 \rightarrow P_3 S$
- $P_6 \rightarrow P_5 B$
- $P_7 \rightarrow P_3 B$

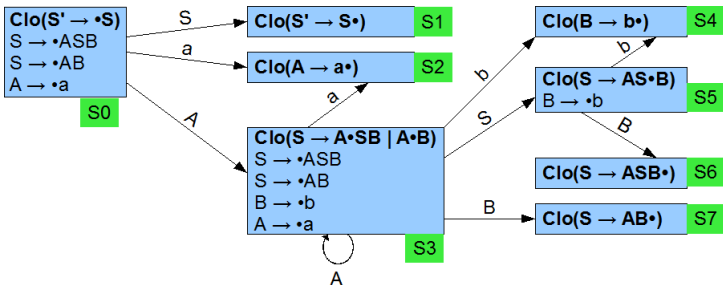


Automaton for left contexts



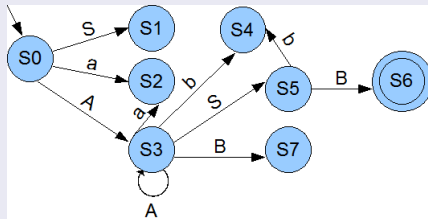
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Same structure, final state = state we want the context for.



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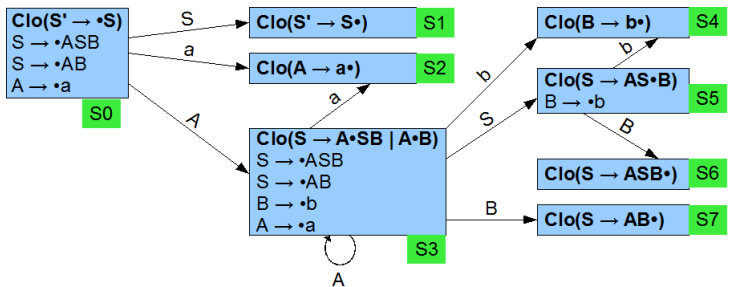
Same structure, final state = state we want the context for.



DR-automata

Gist

- We keep states-track on the stack in every step
- We need the state only while reducing to **determine the final state**
- The β -table is potentially large and is used only after a reduce
- Let's **dismiss** both table and trace and determine state from stack

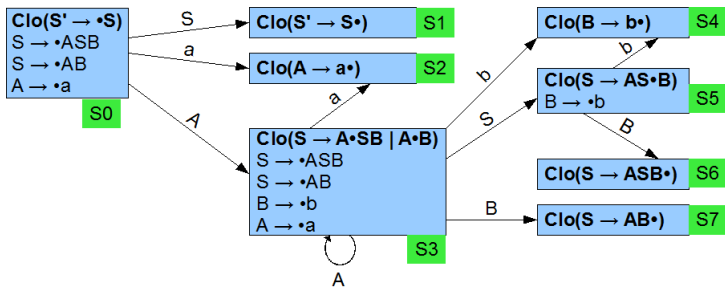


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[A b]

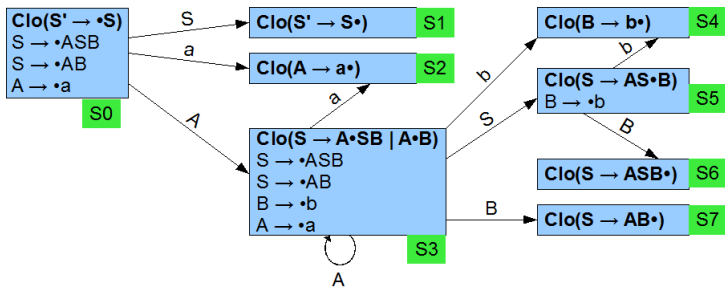


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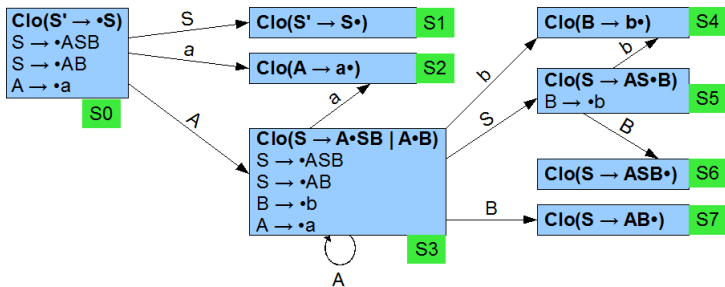


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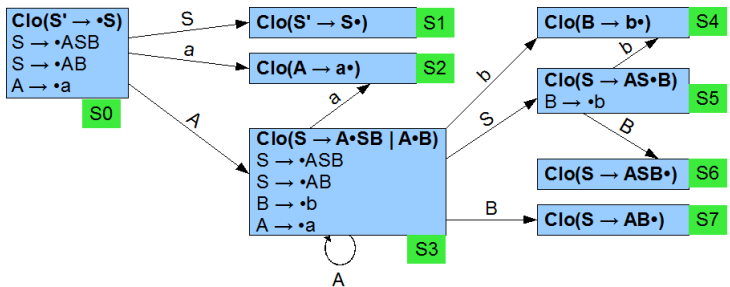


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$[A b] \Rightarrow S4$; $[A a] \Rightarrow S2$;

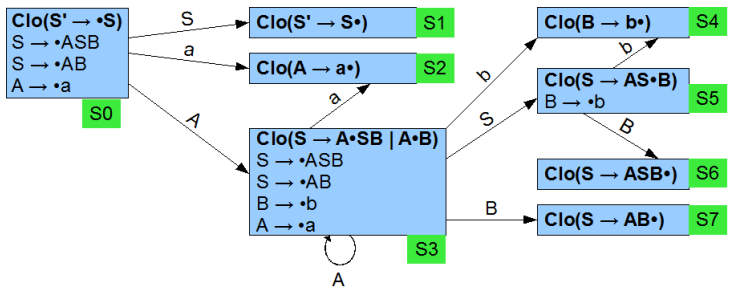


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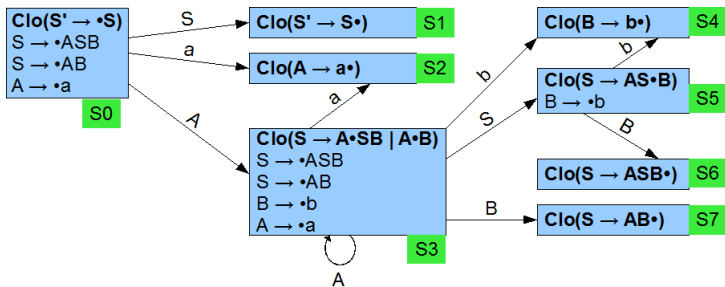


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$[A b] \Rightarrow S4$; $[A a] \Rightarrow S2$; $[A B] \Rightarrow S5$;



Simple approach - problems

- The whole stack is searched, which can be very expensive
- Searching the stack from the top is much more convenient

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DR-state

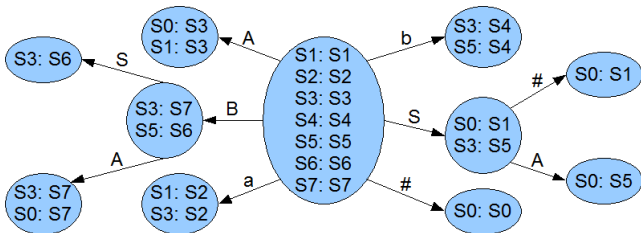
- A set of pairs $S_A : S_B$ with the meaning that a transition $S_A \rightarrow S_B$ is possible by some set of symbols
- Through transitions by stack items, we will try to reduce the set so that only one state appears on the right side = the top state

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Summary

DR-automaton

- From initial state, $|N \cup T|$ arrows fan out, but the latter states have significantly less amount of transitions
- Is created on the basis of the LR-automaton states and transitions
- Is generally smaller (in memory) but slower (in performance) than GOTO table

DR-parsing

- Is generally a bit slower (in performance), but smaller (in memory) than LR
- Doesn't need the states to be tracked on the stack
- Uses a DR-automaton instead of a GOTO table to determine final state after reduction

Right Context

Definition, attributes

- Set of terminal strings that can appear in the input
- Bound to **items**
- No longer regular, rather **context-free**
- Dot right context $F_1\{I\}$ vs. item right context $D_1\{I\}$

- $S \rightarrow aBb$

- $S \rightarrow aCc$

- $B, C \rightarrow \epsilon$

- $F_x\{B \rightarrow \circ\} = \{b\}$

- $F_x\{C \rightarrow \circ\} = \{c\}$

Computing right contexts

■ Item RC

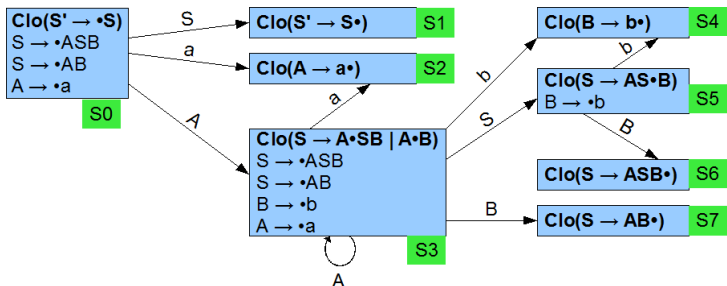
- $F_x\{A \rightarrow \circ\alpha\} \rightarrow \gamma F_x\{X \rightarrow \beta \circ A\gamma\}$

- $F_x\{A \rightarrow \alpha t \circ \beta\} \rightarrow F_y\{A \rightarrow \alpha \circ t\beta\}$

■ Dot RC

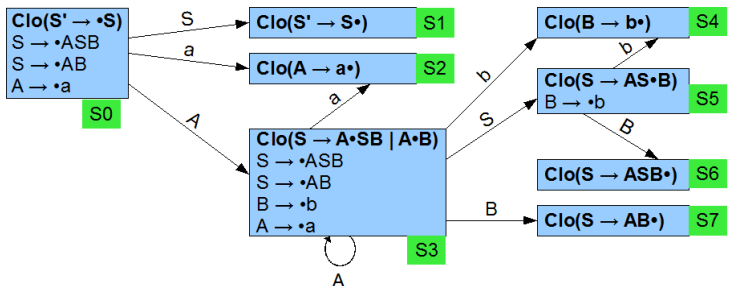
- $D_x\{A \rightarrow \alpha \circ \beta\} \rightarrow \beta F_x\{A \rightarrow \alpha \circ \beta\}$

Right context - example



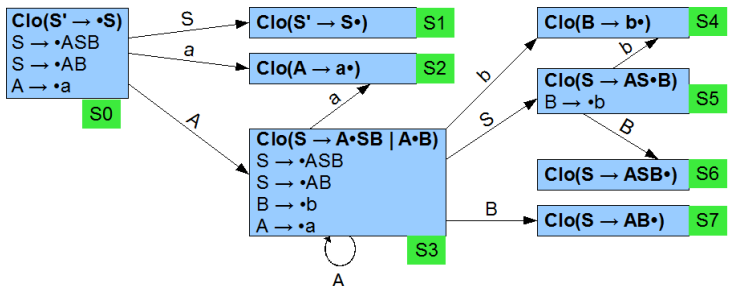
■ $F_{S_0}\{S' \rightarrow \circ S\} = \epsilon$

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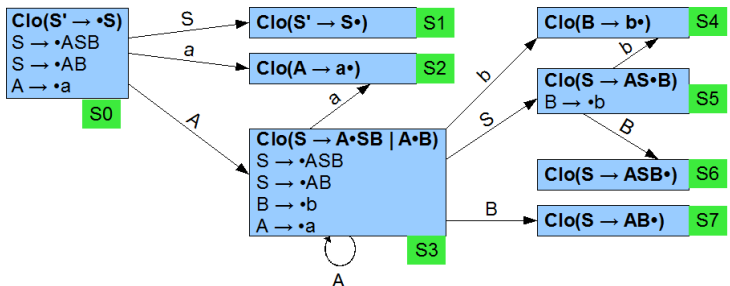
- $F_{S_0}\{S' \rightarrow \circ S\} = \epsilon$
- $F_{S_0}\{S \rightarrow \circ ASB\} = F_{S_0}\{S' \rightarrow \circ S\}$
- $F_{S_0}\{S \rightarrow \circ AB\} = F_{S_0}\{S' \rightarrow \circ S\}$
- $F_{S_0}\{A \rightarrow \circ a\} = B F_{S_0}\{S \rightarrow \circ AB\}$
- $F_{S_0}\{A \rightarrow \circ a\} = SB F_{S_0}\{S \rightarrow \circ ASB\}$

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- $F_{S_0}\{A \rightarrow \circ a\} = SB F_{S_0}\{S \rightarrow \circ ASB\}$
- $F_{S_1}\{S' \rightarrow S\circ\} = F_{S_0}\{S' \rightarrow \circ S\}$
- $F_{S_2}\{A \rightarrow a\circ\} = F_{S_0}\{A \rightarrow \circ A\}$

Right context - example



- $F_{S0}\{S' \rightarrow \circ S\} = \epsilon$
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- $F_{S1}\{S' \rightarrow S \circ\} = F_{S0}\{S' \rightarrow \circ S\}$
- $F_{S2}\{A \rightarrow a \circ\} = F_{S0}\{A \rightarrow \circ A\}$
- $D_{S0}\{S' \rightarrow \circ S\} = S F_{S0}\{S' \rightarrow \circ S\}$
- $D_{S0}\{S \rightarrow \circ ASB\} = ASB F_{S0}\{S \rightarrow \circ ASB\}$

LR-Regular parsing

Right contexts

- Right contexts = super look-ahead
- May be helpful when dealing with inadequate states
- However, intersection of CFG's is undecidable
- Checking the rest of the input against CFG makes no sense

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LR-Regular

- Uses **regular envelopes** of the right contexts
- Approximation "from above"
- For non-terminals only
- Many heuristics and techniques possible, result is not guaranteed

Thank you for your attention.
Questions?