Light Transport Simulation: From Basics to Advanced

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Light Transport Simulation – Motivation I.





Figure: Photography or render?

Light Transport Simulation – Motivation II.



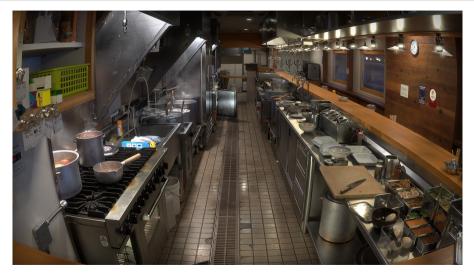


Figure: Photography or render?



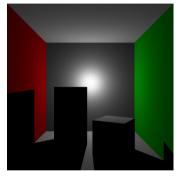


Figure: Photography or render?



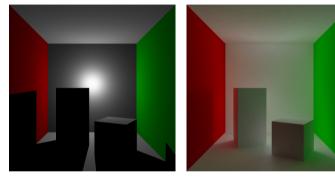






(a) Direct Illumination





(a) Direct Illumination

(b) Indirect Illumination





(a) Direct Illumination

(b) Indirect Illumination

(c) Global Illumination





(a) Direct Illumination

(b) Indirect Illumination

(c) Global Illumination

Global Illumination + Physically Based Shading = (Photo)Realistic Rendering or Physically Based Rendering



- Radiometry overview and BRDF
- 2 Rendering Equation to Light Transport Equation
- 3 Light Transport methods

1st part-Radiometry overview and BRDF

Radiometry overview I.



Radiometry is defined for all kinds of electromagnetic waves, however photometry utilizes only the visible light spectrum, according to the human perception.

radiometry	eng. name	symbol	unit	photometry	eng. name	symbol	unit
zářivá energie	radiant energy	Q_e	J	světelné množství	luminous energy	Q	lm · s
zářivost	radiant intensity	I_e	$W \cdot sr^{-1}$	svítivost	luminous intensity	Ι	cd (kandela)
zářivý tok	radiant flux	ϕ_e	W	světelný tok	luminous flux	ϕ	lm (lumen)
intenzita ozáření	irradiance	E_e	$W \cdot m^{-2}$	osvětlení	illuminance	Ε	lx (lux)
zář	radiance	L_e	$W \cdot sr^{-1} \cdot m^{-2}$	jas	luminance	L	$cd \cdot m^{-2}$
expozice	radiant exposure	H_e	$J \cdot m^{-2} = W \cdot s \cdot m^{-2}$		luminous exposure	H	lx · s
intenzita vyzařování	radiant exitance	M_e	$W \cdot m^{-2}$	intenzita světlení	luminous exitance	M	$\text{Im} \cdot \text{m}^{-2}$
radiozita	radiosity	J_e	$W \cdot m^{-2}$	-	-	-	-

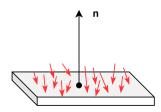
- **Note:** in GI, subscript *"e*" is usually omitted, however it is the only sign that differs them from photometry.
- **Note:** in most cases, subscript *"e*" denotes an emitted radiance (e. g. light sources, derived from radiant intensity).
- Each quantity has a spectral variant.
- Light Transport Simulation utilizes Radiometry.



Radiant flux (zářivý tok)

Radiant flux is an emitted, reflected, transmitted or received radiant energy Q_e per unit frequency t.

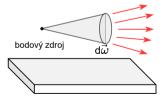
$$\Phi = \frac{\mathrm{d}Q_e}{\mathrm{d}t} \; [\mathsf{W} = \mathsf{J} \cdot \mathsf{s}^{-1}]$$



Radiant intensity (zářivost)

Radiant intensity is the emitted, reflected, transmitted or received radiant flux per solid angle.

$$I(ec{\omega}) = rac{\mathrm{d}\Phi(ec{\omega})}{\mathrm{d}ec{\omega}} [\mathsf{W}\cdot\mathsf{sr}^{-1}]$$

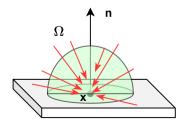


Radiometry overview III.

Irradiance (intenzita ozáření)

Irradiance is the radiant flux received by surface on unit area A. In practice, it is measured in a point \mathbf{x} on the surface.

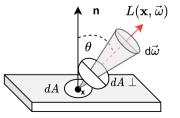
$$E(\mathbf{x}) = rac{\mathrm{d}\Phi(\mathbf{x})}{\mathrm{d}A(\mathbf{x})} [\mathsf{W}\cdot\mathsf{m}^{-2}]$$



Radiance (zář)

Radiance is the emitted, reflected, transmitted or received radiant flux per solid angle $\vec{\omega}$ per unit area A.

$$L(\mathbf{x},\vec{\omega}) = \frac{\mathrm{d}^2 \Phi(\mathbf{x},\vec{\omega})}{\mathrm{d}\vec{\omega} \,\mathrm{d}A(\mathbf{x}) \left(\mathbf{n}\cdot\vec{\omega}\right)} [\mathsf{W}\cdot\mathsf{sr}^{-1}\cdot\mathsf{m}^{-2}]$$





Bidirectional Reflectance Distribution Function: function takes an incoming light direction $\vec{\omega_i}$, and outgoing direction $\vec{\omega_o}$, and returns the ratio of radiance exiting along $\vec{\omega_o}$ to the incident radiance on the surface from direction $\vec{\omega_i}$.

$$f_r(\mathbf{x}, ec{\omega_i}
ightarrow ec{\omega_o}) = rac{\mathrm{d}L_r(\mathbf{x}, ec{\omega_o})}{\mathrm{d}E(\mathbf{x})} = rac{\mathrm{d}L_r(\mathbf{x}, ec{\omega_o})}{L_i(\mathbf{x}, ec{\omega_i}) \cdot \cos(heta_i) \, \mathrm{d}ec{\omega_i}}$$

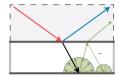
- Mathematical description of surface light interaction properties.
- Intuition: the probability density that photon incoming the surface from direction $\vec{\omega_i}$ will be reflected in direction $\vec{\omega_o}$.
- Also often referenced as BSDF.



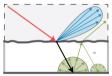
BRDF examples

Smooth diffuse material (diffuse)

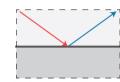
Thin dielectric material (thindielectric)



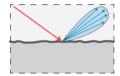
Smooth plastic material (plastic)



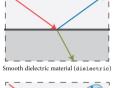
Rough plastic material (roughplastic)

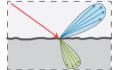


Smooth conducting material (conductor)



Rough conducting material (roughconductor)





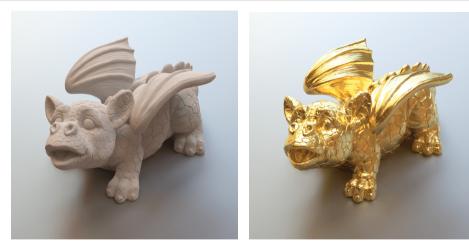
Rough dielectric material (roughdielectric)





BRDF examples





(a) Oren-Nayar BRDF

(b) Torrance-Sparrow BRDF

Figure: BRDF examples

2nd part – Rendering Equation to Light Transport Equation



Rendering equation (Kajiya 1986) in solid angle form:

$$L(\mathbf{x}, \vec{\omega_o}) = L_e(\mathbf{x}, \vec{\omega_o}) + \int_{\Omega} L(\mathbf{x}', -\vec{\omega_i}) f_r(\mathbf{x}, \vec{\omega_i} \to \vec{\omega_o}) \cdot \cos(\theta_i) \mathrm{d}\vec{\omega_i} \quad \text{(sr}^{-1}) \quad \text{(1)}$$

On the contrary, rendering equation in three-point area form:

$$L(\mathbf{x}' \to \mathbf{x}'') = L_e(\mathbf{x}' \to \mathbf{x}'') + \int_M L(\mathbf{x} \to \mathbf{x}') \cdot f_r(\mathbf{x} \to \mathbf{x}' \to \mathbf{x}'') \cdot G(\mathbf{x} \leftrightarrow \mathbf{x}') \, \mathrm{d}A(\mathbf{x})$$
(2)

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Rendering equation (Kajiya 1986) in solid angle form:

$$L(\mathbf{x}, \vec{\omega_o}) = \underbrace{L_e(\mathbf{x}, \vec{\omega_o})}_{\text{emission}} + \int_{\Omega} L(\mathbf{x}', -\vec{\omega_i}) f_r(\mathbf{x}, \vec{\omega_i} \to \vec{\omega_o}) \cdot \cos(\theta_i) d\vec{\omega_i}$$
(1)

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(2)



Rendering equation (Kajiya 1986) in solid angle form:

$$L(\mathbf{x}, \vec{\omega_o}) = L_e(\mathbf{x}, \vec{\omega_o}) + \int_{\Omega} \underbrace{L(\mathbf{x}', -\vec{\omega_i})}_{\text{incoming radiance}} f_r(\mathbf{x}, \vec{\omega_i} \to \vec{\omega_o}) \cdot \cos(\theta_i) d\vec{\omega_i}$$
(1)

On the contrary, rendering equation in three-point area form:

$$L(\mathbf{x}' \to \mathbf{x}'') = L_e(\mathbf{x}' \to \mathbf{x}'') + \int_M L(\mathbf{x} \to \mathbf{x}') \cdot f_r(\mathbf{x} \to \mathbf{x}' \to \mathbf{x}'') \cdot G(\mathbf{x} \leftrightarrow \mathbf{x}') \, \mathrm{d}A(\mathbf{x})$$
(2)

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Rendering equation (Kajiya 1986) in solid angle form:

$$L(\mathbf{x}, \vec{\omega_o}) = L_e(\mathbf{x}, \vec{\omega_o}) + \int_{\Omega} L(\mathbf{x}', -\vec{\omega_i}) \underbrace{\frac{f_r(\mathbf{x}, \vec{\omega_i} \to \vec{\omega_o})}{\text{BRDF coefficient}}}_{\text{BRDF coefficient}} \cdot \cos(\theta_i) d\vec{\omega_i} \tag{1}$$

On the contrary, rendering equation in three-point area form:

$$L(\mathbf{x}' \to \mathbf{x}'') = L_e(\mathbf{x}' \to \mathbf{x}'') + \int_M L(\mathbf{x} \to \mathbf{x}') \cdot f_r(\mathbf{x} \to \mathbf{x}' \to \mathbf{x}'') \cdot G(\mathbf{x} \leftrightarrow \mathbf{x}') \, \mathrm{d}A(\mathbf{x})$$
(2)

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Rendering equation (Kajiya 1986) in solid angle form:

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(1)

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(2)

Light transport equation II. – three point area form



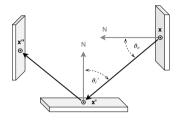


Figure: Three point rendering equation geometry

It remains to define so-called geometric term:

$$G(\mathbf{x} \leftrightarrow \mathbf{x}') = V(\mathbf{x} \leftrightarrow \mathbf{x}') \cdot \frac{|\cos(\theta_o) \cdot \cos(\theta_i')|}{\|\mathbf{x} - \mathbf{x}'\|^2}$$
(3)

Light transport equation III. – recursion and intensity



But recursion is bad...

$$egin{aligned} L &= L_e(x) + \int_M L \, \mathrm{d}A = \ &= L_e(x) + \int_M \left(L_e(x) + \int_M L \, \mathrm{d}A
ight) \, \mathrm{d}A = \ &= L_e(x) + \int_M \left(L_e(x) + \int_M \left(L_e(x) + \int_M L \, \mathrm{d}A
ight) \, \mathrm{d}A
ight) \, \mathrm{d}A = \dots \end{aligned}$$

Intuition: We would like to have a single equation which tells us the intensity I of pixel j ...

Light transport equation III. – recursion and intensity



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ight) \, \mathrm{d}A
ight) \, \mathrm{d}A = \dots \end{aligned}$$

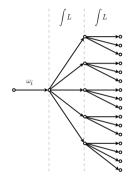
Intuition: We would like to have a single equation which tells us the intensity I of pixel j ...

... therefore, we introduce intensity measurement equation:

$$I_{j} = \int_{M \times M} W_{e}^{j}(\mathbf{x} \to \mathbf{x}') L(\mathbf{x} \to \mathbf{x}') G(\mathbf{x} \leftrightarrow \mathbf{x}') dA(\mathbf{x}) dA(\mathbf{x}')$$
(5)

Light transport equation IV. – path integral

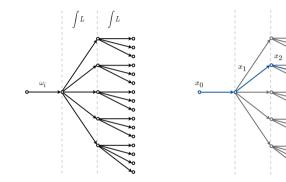




(a) Recursive trajectory principle

Light transport equation IV. – path integral





(a) Recursive trajectory principle

(b) Path integral

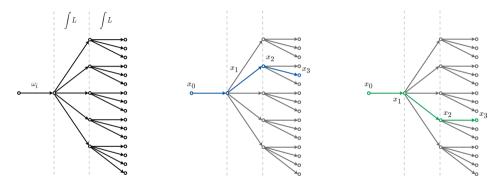
2

 $\rightarrow \circ x_3$

\$

Light transport equation IV. – path integral





(a) Recursive trajectory principle

(b) Path integral

(c) Path integral

Path integral: instead of using a **recursive trajectory principle** (like in rendering equation), path integral uses an **integral over all trajectories**. (Veach 1998)

$$I_{j} = \underbrace{\int_{\Omega}}_{\text{all paths}} \underbrace{f_{j}(\bar{x})}_{\text{throughput function}} d\omega(\mathbf{x})$$
(6)

Imagine integrating the whole recursion tree using rendering equation, the result will be the **same** as integrating over all paths in the tree, if you use correct throughput function.



Using recursive expansion of integral from equation 2 into k dimension wide integral, with omitting the emissive part, and inserting into equation 5, together with applying path integral theorem, the result is following: (Veach 1998)

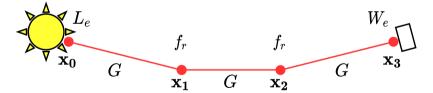
$$egin{aligned} &I_j = \sum_{k=1}^\infty \int_{M^{k+1}} L_e(\mathbf{x}_0 o \mathbf{x}_1) \cdot G(\mathbf{x}_0 o \mathbf{x}_1) \cdot W_e(\mathbf{x}_{k-1} o \mathbf{x}_k) \ &\left(\prod_{i=1}^{k-1} f_r(\mathbf{x}_{i-1} o \mathbf{x}_i o \mathbf{x}_{i+1}) \cdot G(\mathbf{x}_i o \mathbf{x}_{i+1})
ight) \, \mathrm{d}A(\mathbf{x}_0) \dots \mathrm{d}A(\mathbf{x}_k) \end{aligned}$$

Light transport equation VI. – integrand



$$f_{j}(\overline{\mathbf{x}}) = L_{e}(\mathbf{x}_{0} \to \mathbf{x}_{1}) \cdot G(\mathbf{x}_{0} \leftrightarrow \mathbf{x}_{1}) \cdot f_{r}(\mathbf{x}_{0} \to \mathbf{x}_{1} \to \mathbf{x}_{2}) \cdot G(\mathbf{x}_{1} \leftrightarrow \mathbf{x}_{2}) \cdot f_{r}(\mathbf{x}_{1} \to \mathbf{x}_{2} \to \mathbf{x}_{3}) \cdot G(\mathbf{x}_{2} \leftrightarrow \mathbf{x}_{3}) \cdot W_{e}^{j}(\mathbf{x}_{2} \to \mathbf{x}_{3})$$
(8)

An example of integrand, constructed with path $\bar{x} = \mathbf{x}_0 \mathbf{x}_1 \mathbf{x}_2 \mathbf{x}_3$





Monte Carlo integration

A function $f: \Omega \rightarrow \mathbf{R}$ can be estimated using Monte Carlo method with N random samples as:

$$I = \int_{\Omega} f(x) \mathrm{d}x \approx \frac{1}{N} \sum_{i=1}^{N} \frac{f(x_i)}{p(x_i)}, \qquad (9)$$

where x_i is a random variable with probability density function $p(x_i)$.

3rd part-Light Transport methods



unidirectional	bidirectional	hybrids		
Particle Tracing	Bidirectional	Metropolis Light		
Particle fracing	Path Tracing	Transport		
Path Tracing	Photon Mapping	Energy Redistribution		
Fain fracing	and variants	Path Tracing		
	Vertex Connections			
	and Merging			
	Virtual Point Lights			

Possible solutions



Most of the methods are based on ray tracing principle

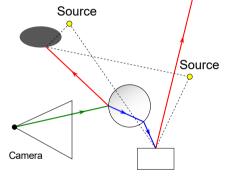
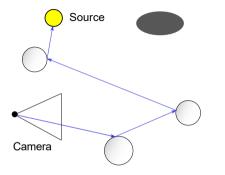


Figure: Ray tracing

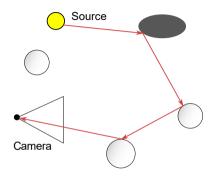
... which is NOT global illumination method

Ray tracing based methods





(a) **path tracing** – backward tracing from camera to the light source

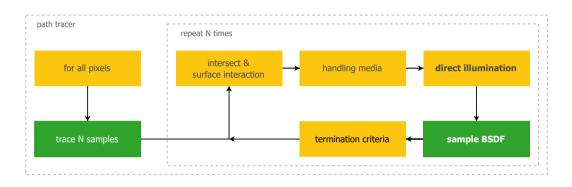


(b) **light tracing** – forward tracing from light source to the camera

Figure: Forward/backward tracing comparison

Path tracer pipeline





- Cheated Path Tracing also present in modern games: Cyberpunk, Witcher 3,
- NVIDIA SDK for real-time PT:

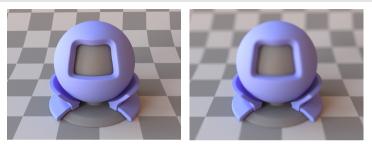
https://developer.nvidia.com/rtx/path-tracing

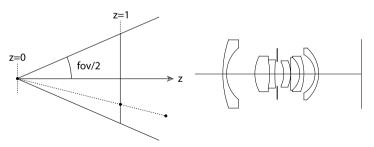
Designing path tracer I. – Camera sample



Generalized algorithm:

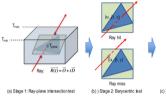
- Sample sensor (film)
- 2 Sample lens
- 3 Cast a ray
 - Pinhole camera has infinitely small aperture, infinite depth of field.
- Realistic lens-tracing ray through optical system.





Designing path tracer II. – Intersect & Surface interaction | 🖬 🎹

Intersect with scene (traverse BVH, bounding box, kD, etc.)

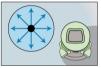




(c)) Stage 3: Exact hit point calculation

- If no hit, try to shade using surrounding lights
- 3 Check for direct light source hit
- 4 Prepare BSDF

Standard emitters





Point emitter (point)

Area emitter (area)

Environment emitters





Environment map emitter (envmap)

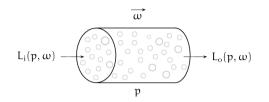
Constant environment emitter (constant)

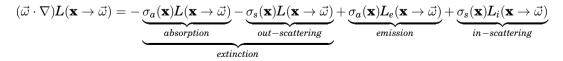
Image taken from Mitsuba 3 doc.

Designing path tracer III. – Handling media



- Except of surface interaction, there can be medium interaction
- Participating medium is a black box for solving volume mediums or subsurface scattering (fog, human skin, wax, liquids, ...)
- Scatter inside medium.
- 2 Solve Radiative Transfer Equation
- 3 Return to path tracer
- RTE can be solved with Ray Marching inside medium





Designing path tracer IV. – Direct illumination



- Shadow ray from each path vertex towards a random light source.
- Only for **NON**-pure specular surfaces.
- How to handle the ray orientation?
- How to evaluate weight w?

Algorithm:

- 1 Pick random light source with selection PDF p_s .
- ${\color{black} 2}$ Sample emitter with PDF p_{em}
- 3 Check visibility
- 4 Eval contribution: $th \cdot f_s \cdot L_e \cdot w(p_s, p_{em}, p_{fs})$

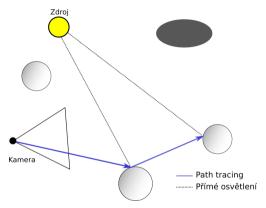


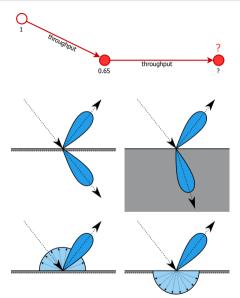
Figure: Path tracing with direct illumination

... also called Next Event Estimation (NEE)

Designing path tracer V. – Sampling



- Pick any BSDF component to sample.
- 2 Compute BSDF value f_s
- 3 Sample new outgoing direction $\vec{\omega_o}$ with PDF p_{fs} .
- **4** Update throughput: $th = th \cdot f_s$.
- Possible interactions:
 - reflect (mirror, glossy, dielectrics, plastics)
 - refract (dielectrics, plastics)
 - scatter (matte, plastics)
- Materials can be smooth or rough (microfacet models)
- Importance sample direction with respect to BSDF shape.

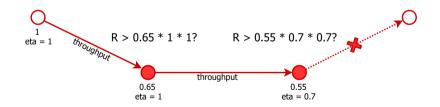


Designing path tracer VI. – Termination criteria

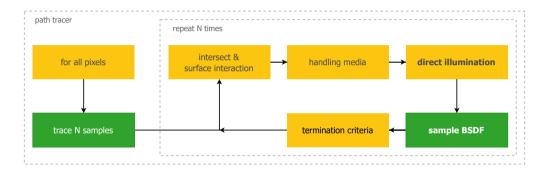




- How to prevent too long paths? E.g due to total internal reflection.
- Fixed path length
- Russian roulette
- The lower throughput, the higher termination chance



Designing path tracer VII. – Entire pipeline



- Similar approach can be applied to particle/light tracing.
- We can achieve faster convergence with De-noisers, Path Guiding, ...

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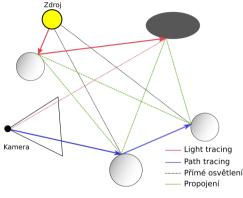
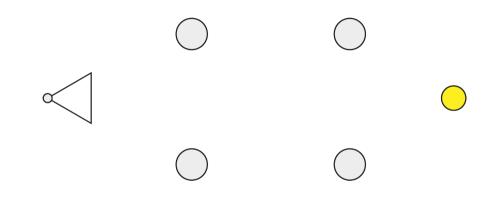


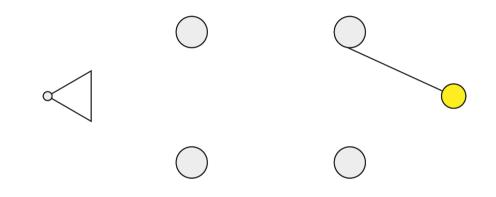
Figure: Bidirectional Path Tracing

Bidirectional path tracing (Veach 1998) is considered to be one of the most powerful "basic" algorithms.

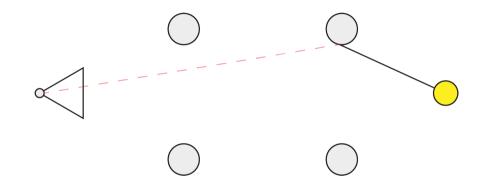




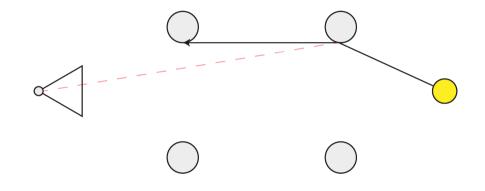




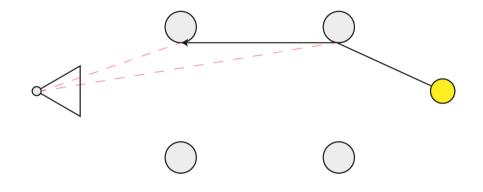




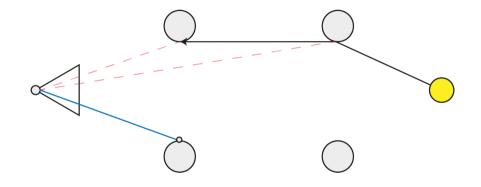




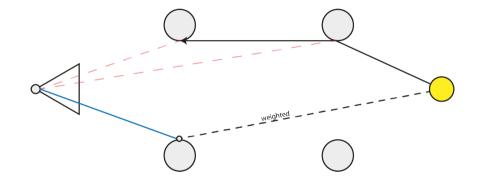




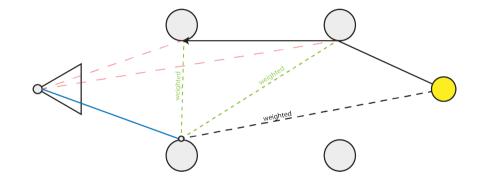




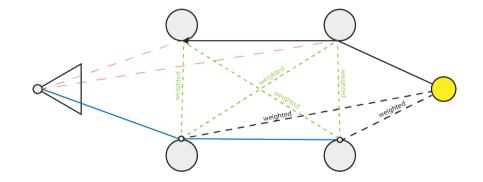






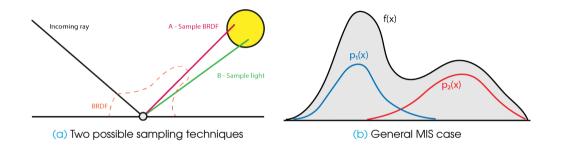






Multiple Importance Sampling





MIS is a powerful noise reduction tool:

$$w_s(\mathbf{x}) = \frac{n_s \cdot p_s(\mathbf{x})}{\sum_i n_i \cdot p_i(\mathbf{x})}$$
(10)

This strategy is called balance heuristic.





(a) LT (b) PT (c) PT + DI (d) BDPT (e) BDPT + MIS

Figure: PT vs BDPT, all images uses x60 supersampling

PT vs BDPT



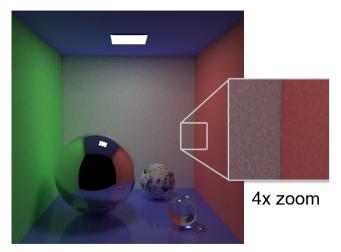


Figure: BDPT + MIS



BDPT is more powerfull than PT but ...

- Quite complicated to implement.
- PT is more simple for mass parallel acceleration on GPU and more friendly.
- Modern rendering systems are based on PT + NEE (Next-Event-Estimation) + denoise + path guiding + post-processing.
- Multiple Importance Sampling (MIS) is applicable also on PT.



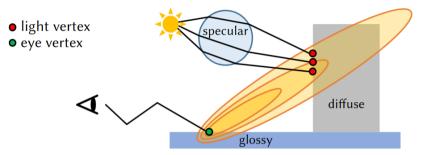
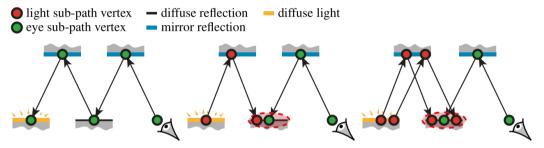


Figure: Unconnected GDS path

Unbiased algorithms like PT or BDPT can't efficiently handle SDS, GDS, SGD, GDG paths (S–Specular, G–Glossy, D–Diffuse)



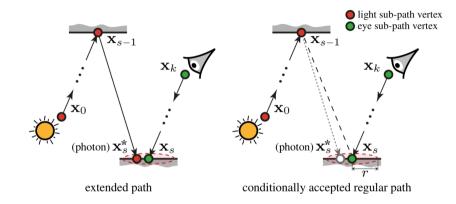


unidirectional sampling vertex merging (no path reuse) vertex merging (path reuse) Figure: Left: unidirectional sampling. Middle: vertex merging. Right: light path re-using.

Combination of BDPT and Photon Mapping (Georgiev et al. 2012), via multiple importance sampling in path space domain.

Vertex Connections and Merging





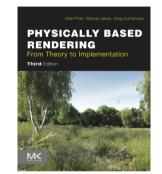
- Requires spatial structure with range-search support.
- Original implementation uses hash grid.

Open source and scientific implementations



- Physically Based Rendering (Pharr, Jakob, and Humphreys 2016)
- Mitsuba 3 (Jakob et al. 2022)

Most of the scientific papers are implemented in one of these.







What we discussed today:

- Basics to Radiometry and BRDF/BSDF
- Rendering equation and Light Transport Equation
- Stochastic solution to RE/LTE
- Path Tracing
- Bidirectional Path Tracing and Multiple Importance Sampling
- Vertex Connections and Merging



Where else to look ...

- Photon mapping and its variants (PM, PPM, SPPM)
- Metropolis light transport (MLT)
- Energy redistribution path tracing (PT + MLT)

• ...

- Acceleration methods (Path guiding, Hierarchical Russian roulette, Quasi-Monte Carlo)
- Differentiable rendering
- Spectral rendering
- Signed Distance Fields in LTS

T FIT

Sources

- Georgiev, Iliyan et al. (Nov. 2012). "Light Transport Simulation with Vertex Connection and Merging". In: ACM Trans. Graph. 31.6, 192:1–192:10. ISSN: 0730-0301.
- Jakob, Wenzel et al. (2022). Mitsuba 3 renderer. Version 3.0.1. https://mitsuba-renderer.org.
- Kajiya, James T. (Aug. 1986). "The Rendering Equation". In: Proceedings of the 13th Annual Conference on Computer Graphics and Interactive Techniques. Vol. 20. SIGGRAPH '86 4. New York, NY, USA: ACM, pp. 143–150. ISBN: 0-89791-196-2.
- Pharr, Matt, Wenzel Jakob, and Greg Humphreys (2016). Physically Based Rendering: From Theory to Implementation. 3rd. San Francisco, CA, USA: Morgan Kaufmann Publishers Inc. ISBN: 0128006455.
- Veach, Eric (1998). "Robust Monte Carlo Methods for Light Transport Simulation". PhD thesis. Stanford, CA, USA. ISBN: 0591907801.

Thank you for attention